

COMPARING AND SCALING Ratios, Rates, Percents, and Proportions

<p>Instructional Time and Investigations</p>	<p>22 days</p>	<ul style="list-style-type: none"> • Inv. 1: Ways of Comparing: Ratios and Proportions (4 Problems) • Inv. 2: Comparing and Scaling Rates (3 Problems) • Inv. 3: Markups, Markdowns, and Measures: Using Ratios, Percents, and Proportions (3 Problems) 	
<p>Goals</p>	<p>Ratios, Rates, and Percents: Understand ratios, rates, and percents.</p> <ul style="list-style-type: none"> • Ratios make comparisons between two quantities. Rates, unit rates, and percents are all types of ratios. • Knowing the desired ratio between two variables allows you to scale the ratio or find a missing part of a ratio. 	<p>Proportionality: Understand proportionality in tables, graphs, and equations.</p> <ul style="list-style-type: none"> • A proportional relationship has particular characteristics when represented in a table, graph or equation. For example, it is a straight line in a graph and can be represented as $y = mx$. 	<p>Reasoning Proportionality: Develop and use strategies for solving problems that require proportional reasoning.</p> <ul style="list-style-type: none"> • Being able to change the form of a ratio is a useful problem-solving strategy. • Various strategies can be used to solve problems involving proportions, including scaling, rate tables, percent bars, unit rates, and equivalent ratios.
<p>Common Core Standards</p>	<p>Common Core Standards for Mathematical Practice</p> <p>MP.1: Make sense of problems and persevere in solving them.</p> <p>MP.2: Reason abstractly and quantitatively.</p> <p>MP.3: Construct viable arguments and critique the reasoning of others.</p> <p>MP.4: Model with mathematics.</p> <p>MP.5: Use appropriate tools strategically.</p> <p>MP.6: Attend to precision.</p> <p>MP.7: Look for and make use of structure.</p> <p>MP.8: Look for and express regularity in repeated reasoning.</p>	<p>Common Core Content Standards</p> <p>7.RP.A.1: Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units.</p> <p>7.RP.A.2: Recognize and represent proportional relationships between quantities.</p> <p>7.RP.A.3: Use proportional relationships to solve multistep ratio and percent problems.</p> <p>7.EE.B.4 Use variables to represent quantities in a real-world or mathematical problem, and construct simple equations and inequalities to solve problems by reasoning about the quantities.</p> <p>Also 7.RP.A.2a–d, 7.NS.A.3, 7.EE.A.2, 7.EE.B.3, 7.EE.B.4a</p>	

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Content Connections to Other Units

Goals of the Unit	Prior Work	Future Work
<p>Ratios, Rates, and Percents: Understand ratios, rates, and percents.</p>	<ul style="list-style-type: none"> Exploring and applying rational number concepts (<i>Comparing Bits and Pieces; Let's Be Rational; Decimal Ops; Accentuate the Negative</i>) Percent defined as a ratio to 100 and connected to fractions and decimals (<i>Comparing Bits and Pieces; Let's Be Rational; Decimal Ops</i>) 	<ul style="list-style-type: none"> Calculating and applying slope with equations in $y = mx + b$ form (<i>Moving Straight Ahead; Thinking With Mathematical Models; Say It With Symbols</i>) Making comparisons between groups of different sizes (<i>Samples and Populations; Growing, Growing, Growing</i>)
<p>Proportionality: Understand proportionality in tables, graphs, and equations.</p>	<ul style="list-style-type: none"> Connecting and comparing rates using ratios, decimals, and percents (<i>Comparing Bits and Pieces; Let's Be Rational; Stretching and Shrinking</i>) Comparing data sets (<i>Data About Us</i>) Representing patterns of change in words, tables, graphs, and equations (<i>Variables and Patterns</i>) Fractions as a part/whole comparison, addition, subtraction, multiplication, and division with fractions (<i>Comparing Bits and Pieces; Let's Be Rational</i>) 	<ul style="list-style-type: none"> Comparing probabilities (<i>What Do You Expect?</i>) Comparing data sets (<i>Samples and Populations; Thinking With Mathematical Models</i>) Finding the equation of a line (<i>Moving Straight Ahead; Thinking With Mathematical Models</i>) Expressing linear relationships with symbols (<i>Moving Straight Ahead; Thinking With Mathematical Models; Growing, Growing, Growing</i>) Expressing and applying probabilities as fractions (<i>What Do You Expect?</i>) Determining if two algebraic expressions are equivalent (<i>Growing, Growing, Growing; Frogs, Fleas and Painted Cubes; Say It With Symbols; Function Junction</i>)
<p>Reasoning Proportionality: Develop and use strategies for solving problems that require proportional reasoning.</p>	<ul style="list-style-type: none"> Using percents to make comparisons (<i>Comparing Bits and Pieces; Decimal Ops</i>) Recognizing direct proportionality relationships with a unit rate (<i>Variables and Patterns</i>) Making inferences about quantities (<i>Data About Us</i>) Comparing and subdividing similar figures to determine scale factors (<i>Stretching and Shrinking</i>) 	<ul style="list-style-type: none"> Expressing proportional and nonproportional linear relationships with symbols (<i>Moving Straight Ahead; Thinking With Mathematical Models</i>) Making inferences about quantities and populations based on experimental or theoretical probabilities (<i>What Do You Expect?</i>) Estimating with and comparing large numbers (<i>Growing, Growing, Growing</i>) Developing benchmarks and skills for estimating irrational numbers (<i>Looking for Pythagoras</i>) and for estimating populations (<i>Samples and Populations</i>) Scaling up rectangular prisms (<i>Filling and Wrapping</i>)